

## Threshold power of 1.2 $\mu\text{m}$ infrared laser by in-band pumped $\text{Ho}^{3+}$ -doped crystal

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**Abstract:** The threshold power of 1.2  $\mu\text{m}$  laser generated from the  $\text{Ho}^{3+}$ :LLF crystal was discussed. Two typical quasi-three-level theoretical models were used to analyze the effectiveness of 1194 nm laser's threshold power in the in-band pumping source of 1.15  $\mu\text{m}$  fiber laser with different parameters, such as the absorption coefficient of laser medium, the laser beam radius, the crystal length and reflectivity of the output mirror. It was found that the re-absorption loss was the most important factor leading to the different results for the two models, and the second model was close to the practice because of the narrow bandwidth pumping beam (<6 nm). The results provided reliable data of  $\text{Ho}^{3+}$ -doped 1.2  $\mu\text{m}$  solid-state laser systems for the design and experimental research in further.

**Key words:** 1.2  $\mu\text{m}$  infrared laser, in-band pumped,  $\text{Ho}^{3+}$ -doped crystal, threshold power

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## 同带泵浦 $\text{Ho}^{3+}$ 激光晶体 1.2 $\mu\text{m}$ 波段红外激光阈值功率

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**摘要:** 为探索同带泵浦掺杂  $\text{Ho}^{3+}$  激光晶体 1.2  $\mu\text{m}$  波段红外激光输出, 采用掺杂浓度为 1 at% 的  $\text{Ho}^{3+}$ :LLF 激光晶体作为激光增益介质, 应用两种典型准三能级理论模型, 计算了  $\text{Ho}^{3+}$  在  $^5\text{I}_6$  和  $^5\text{I}_8$  能级间跃迁辐射 1.19  $\mu\text{m}$  激光的阈值功率, 分析了泵浦光和激光束腰半径、激光晶体长度、吸收损耗、腔镜反射率等参量与阈值功率的变化关系, 得出了吸收损耗是影响阈值功率最敏感因素的重要结论, 确定了泵浦阈值功率的范围, 为后续 1.2  $\mu\text{m}$  波段红外激光实验研究提供了可靠的理论参考数据。

**关键词:** 1.2  $\mu\text{m}$  红外激光; 同带泵浦;  $\text{Ho}^{3+}$  激光晶体; 阈值功率

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### Introduction

With the development of optical mediums and laser technologies, many new lasers have been investigated and applied in various fields<sup>[1]</sup>. The beams, which possess the spectral region from 1.1  $\mu\text{m}$  to 1.2  $\mu\text{m}$ , have attracted much attention because of the pumping sources and the fundamental lights of yellow beams<sup>[2]</sup>. In recent

years, many studies have reported that 1.1 ~ 1.2  $\mu\text{m}$  coherent lights can pump  $\text{Tm}^{3+}$ - $\text{Ho}^{3+}$ -co-doped fiber lasers<sup>[3]</sup>, and many frequency doubled lasers (576 nm, 577 nm, 589 nm, 592 nm) were applied in the domain of astronomy, bio-medicine, cosmetology, high resolution spectroscopy<sup>[4]</sup>. Generally speaking, 1.2  $\mu\text{m}$  lasers can be generated from  $\text{Yb}^{3+}$ -doped fiber lasers, Raman solid-state lasers, diode lasers, He-Ne gas lasers<sup>[5]</sup>, and so on. As we known,  $\text{Ho}^{3+}$ -doped gain mediums are fa-

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mous for working on 2  $\mu\text{m}$ <sup>[6]</sup>. In fact, they are also promising candidates for 1.2  $\mu\text{m}$  coherent sources because  $\text{Ho}^{3+}$  ions can emit plenty of spectral lines in the range from visible to infrared. Recently, Arizona University reported a series of CW and Q-switched 1.2  $\mu\text{m}$  lasers generated from the  $\text{Ho}^{3+}$ -ZBLAN fibers. For example, Zhu *et al.* firstly reported a 1200 nm single-frequency laser from the  $\text{Ho}^{3+}$ -ZBLAN fiber in 2012<sup>[7]</sup> and the 1200 nm laser's power had been increased to Watt-level in 2014<sup>[8]</sup>. In 2015, a 0.44  $\mu\text{J}$  - 5.7  $\mu\text{s}$  - 1190 nm laser was generated by means of a graphene Q-switched short-length holmium-doped ZBLAN fiber<sup>[9]</sup>. However, there are few reports on the 1.2  $\mu\text{m}$  holmium-doped solid-state laser system. Among many rare earth ions doped crystals,  $\text{Ho}^{3+}$ -doped fluoride crystals are of good characteristics of the low phonon energy and thermal lens effects, which is similar to the  $\text{Ho}^{3+}$ -ZBLAN fibers. In this work, a 1 at%  $\text{Ho}^{3+}$ :LLF crystal was firstly chosen as an example for emitting the 1.19  $\mu\text{m}$  laser, and a 1.15  $\mu\text{m}$  fiber laser served as the pumping source. According to the quasi-three levels theory<sup>[10]</sup>, two typical theoretical models were adopted to analyze the threshold power with different parameters. The results demonstrated that the crystal's re-absorption loss is the most important parameter influencing on the threshold power, and all of the theoretical results can be beneficial to further experiment research in future.

## 1 Calculation with Two Models

As shown in Fig. 1, the 1.2  $\mu\text{m}$  fluorescence spectrum can be generated by  $\text{Ho}^{3+}$  ions transmitting from the energy level  $^5\text{I}_6$  to  $^5\text{I}_8$ , which belongs to a quasi-three level system. Compared with the four level systems, many activation ions always stay in the low laser level  $^5\text{I}_8$  in this system. In addition, the serious re-absorption loss can further result in the high threshold pumping power and the low efficiency. Therefore, it is quite necessary to analyze the influence of the re-absorption loss on the pumping threshold power.

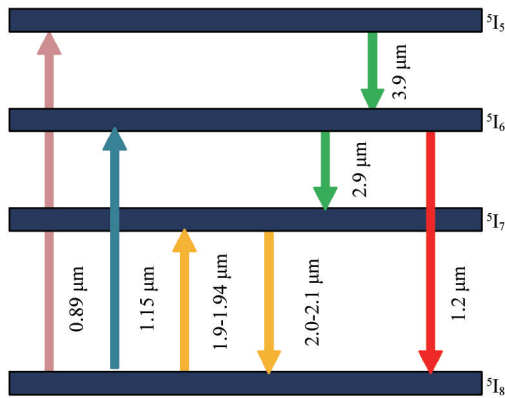


Fig. 1 Partial energy level of  $\text{Ho}^{3+}$ -doped crystal  
图 1 掺杂  $\text{Ho}^{3+}$  离子晶体部分能级图

The first typical quasi-three-level equations were described as follows<sup>[11]</sup>.

$$dN_2(r, z)/dt = f_2 Rr_p(r, z) - [N_2(r, z) - N_2^0]/\tau - \{f_2 c\sigma [N_2(r, z) - N_1(r, z)]/n\} \phi\phi_0(r, z), \quad (1)$$

$$dN_1(r, z)/dt = -f_1 Rr_p(r, z) - [N_1(r, z) - N_1^0]/\tau + \{f_1 c\sigma [N_2(r, z) - N_1(r, z)]/n\} \phi\phi_0(r, z), \quad (2)$$

$$d\phi/dt = (c\sigma/n) \iiint \Delta N(r, z) \phi\phi_0(r, z) dV - \phi c(L + T)/(2nl), \quad (3)$$

where  $N_2$  and  $N_1$  are the actual population density in the upper and lower laser levels, respectively.  $N_1^0$  and  $N_2^0$  are the un-pumped population density.  $f_1$  and  $f_2$  are the Boltzmann constants for the laser lower and upper energy levels, respectively.  $\sigma$  is the emission cross section.  $\tau$  is the lifetime of upper energy level.  $L + T$  is the round-trip loss.  $l$  is the crystal length.  $\sigma$  is the photon density in the resonator.  $r_p(r, z)$  and  $\phi_0(r, z)$  are normalized spatial distribution functions for the pumping light and the laser beam.  $n$  is the crystal's refractive index.  $\Delta N(r, z)$  is the population inversion density.

$$\Delta N(r, z) = \{\tau(f_1 + f_2)Rr_p(r, z) - N_1^0\} / [1 + c\sigma\tau(f_1 + f_2)\phi\phi_0(r, z)/n]. \quad (4)$$

By means of the equations above, the threshold power could be obtained.

$$P_{th} = [\pi h\nu_p(\omega_l^2 + \omega_p^2)(L + T + 2\sigma N_1^0 l)] / (4\sigma\tau\eta_a f), \quad (5)$$

$$f = f_1 + f_2, \quad (6)$$

where  $\eta_a$  is the absorption efficiency.  $h$  is the plank constant.  $\nu_p$  is the frequency of pumping light.  $\omega_l$  and  $\omega_p$  are beam radius on the laser crystal for the coherent laser and the pumping light, respectively.

For the parameters above,  $N_1^0$  is usually regarded as the total activation particles' density in some articles<sup>[20]</sup>. While in some other reports, it is the population density only in the low laser level. Here, it was considered as the former one so as to compare with the following calculation model.

Different from the first model, another threshold power formula is shown in the following expressions<sup>[12]</sup>.

$$P_{th} = [\pi h\nu_p(L/2 + T/2 + g_u f_1 \sigma N_1^0 l/g_d)] / [2\sigma\tau\alpha\eta_p \eta_s (f_2 + g_u f_1/g_d) F(L, \omega_l, \omega_p)], \quad (7)$$

$$F(L, \omega_{(l)}, \omega_p) = \int_0^L \exp(-\alpha z) dz / [\omega_l^2(z) + \omega_p^2(z)], \quad (8)$$

where  $\eta_p$  is the quantum efficiency.  $\omega_l(z)$  and  $\omega_p(z)$  are the pumping light and coherent lasers' beam radius at  $z$  position.  $g_u$  is the laser upper level's energy degeneracy, and  $g_d$  is the laser lower level's energy degeneracy.

By comparing with the above two models, some differences could be found as follows: I) The energy degeneracy  $g_u$  and  $g_d$  were introduced into the re-absorption loss and the Boltzmann constants in the second model. II) The quantum efficiency  $\eta_p$  and the Stokes shift efficiency appeared in the model two, where  $\eta_p = 1$  and  $\eta_s = \lambda_p/\lambda_s = 0.966$ . The wavelengths of the pumping light and the coherent light were 1152 nm and 1194 nm, respectively. It can be seen that  $\eta_p$  and  $\eta_s$  hardly resulted in decisive disparity for the two models. III) The 1152 nm and 1194 nm beams' radii were not concrete values in the second model, and the optical field distribution in

the laser medium was considered<sup>[22]</sup>, while the beams' radii were constants in the first model. IV) The most important factor was that the laser lower energy level's Boltzmann constant  $f_1$  was introduced into the re-absorption loss in the second model, which greatly decreased the threshold power value, while  $N_1^0$  is the total particle number density in the first model.

## 2 Discussion and Results

Both the two models were usually adopted in the quasi-three-level laser design. In order to discuss the re-absorption loss, we calculated the 1.2  $\mu\text{m}$  laser's threshold power and analyzed the influencing factors by using the two models mentioned above. According to the  $\text{Ho}^{3+}$  absorption characteristics<sup>[17]</sup>, the pumping laser's wavelength was determined by 1152 nm belonging to the same band with the 1194 nm coherent light, and the absorption efficiency was about 1. The pumping light and the laser beam were of the same wave radius. The parameters used for calculation were listed in Table 1. The Boltzmann constants for the laser lower and upper energy levels were obtained by the stark energies of  $^3\text{I}_6$  and  $^5\text{I}_8$ .

After the calculations and simulations, the relationship of the absorption coefficient  $\alpha$  and the threshold pumping power  $P_{th}$  were illustrated in Fig. 2a and Fig. 2b, respectively.

Figures 2(a-b) plotted the results of the mode one and mode two, respectively. They had the same changing law under the same condition. When the absorption coefficient exceeded  $0.6 \text{ cm}^{-1}$ , the  $P_{th}$  changed slowly. The smaller the beam radius is, the less the threshold power is. However, the values of the threshold powers are quite different for the two models. The reason can be explained as follows: for one thing, the Boltzmann constant  $f_1$  was included in the model two, but not in model one. For another, the most important factor  $N_1^0$  in the model one and model two had quite different physical meanings. If condition permitted, it is quite necessary to measure the re-absorption loss.

Moreover, the beam radius could be seriously affected by the  $P_{th}$  (Fig. 3). In the model one, the beam radius should be limited within  $50 \mu\text{m}$ , while it could be expanded to several hundreds micrometers in the model two, which would reduce the power density and crystal's damage obviously.

Then the output coupler mirror's reflectivity  $R_2$  with the  $P_{th}$  was simulated in Fig. 4. It could be found that the beam radius values were  $50 \mu\text{m}$  and  $20 \mu\text{m}$ , respectively, in the model one, while  $150 \mu\text{m}$  and  $50 \mu\text{m}$  in the model two. One can see that the threshold power in the model one is always larger than the model two when the wave radii are both  $50 \mu\text{m}$ . In addition, the smaller the beam radius is, the higher the power intensity is, and the easier the laser crystal is damaged. Therefore, the

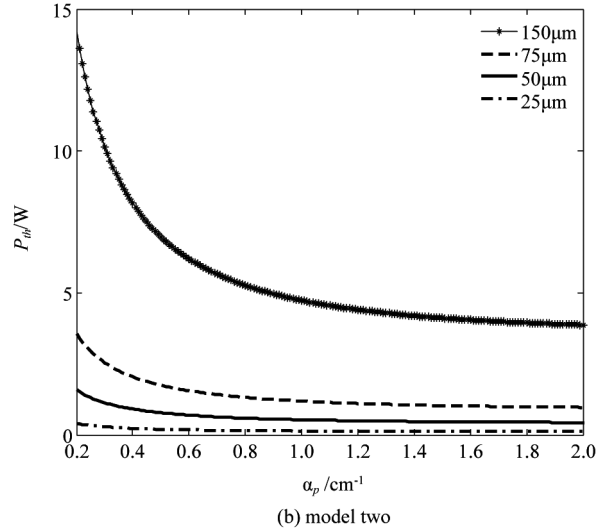
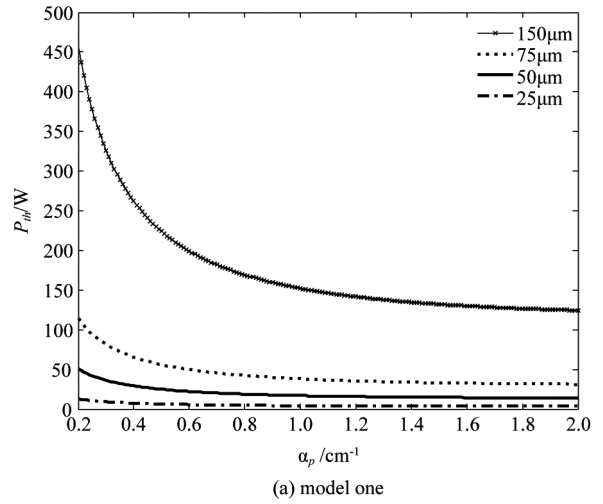


Fig. 2 The relationship of threshold power and absorption coefficient

图2 晶体吸收系数与阈值功率的关系 (a) 模型一 (b) 模型二

beam radius was set at about  $150 \mu\text{m}$  in the model two. The threshold power  $P_{th}$  reduced quickly and is low with increasing of the output mirror's reflectivity  $R_2$ , even there appeared a critical point 76.5%, where the  $P_{th}$  values were equal in the two models.

The laser crystal's length in different models was discussed (Fig. 5). In each model, the optimum length was obtained, which corresponded to the smallest threshold pumping power, and the larger or smaller length could increase the  $P_{th}$  value. As a result, the best length in the model one was 2mm and in the model two was 11 mm.

According to the above discussion, it had a great gap between the two models, and the differences mainly resulted from the re-absorption loss. In the model one, the re-absorption loss is based on the populations in the

Table 1 Parameters for Calculation

表1 计算参数列表

parameters	$h/J \cdot S$	$\lambda_p/\mu\text{m}$	$N/\text{cm}^{-3}$	$\tau/\text{ms}$	$c/\text{m} \cdot \text{s}^{-1}$	$\lambda/\mu\text{m}$	$\sigma_e/\text{cm}^2$	$\sigma_a/\text{cm}^2$	$f_1$	$f_2$
values	$6.63 \times 10^{-34}$	1.15	$1.58 \times 10^{20}$	1.8	$3 \times 10^8$	1.19	$0.85 \times 10^{-20}$	$0.24 \times 10^{-20}$	0.028 8	0.112 2

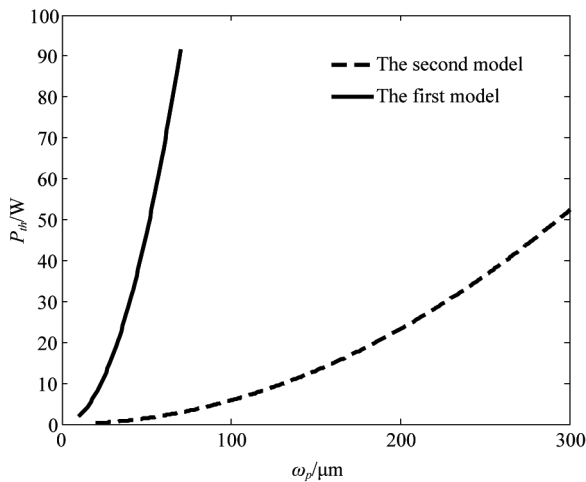


Fig. 3 The relationship of threshold power and beam radius  
图3 光斑半径与阈值功率关系图

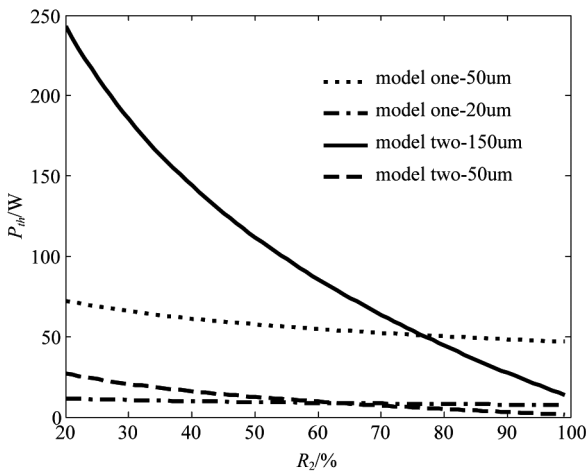


Fig. 4 The threshold power versus reflectivity  
图4 腔镜反射率与阈值功率关系图

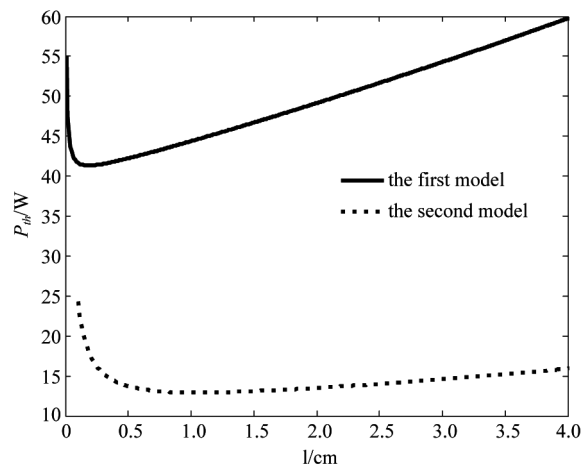


Fig. 5 The threshold power versus laser crystal length  
图5 激光晶体长度与阈值功率关系图

whole ground state level, but in the model two, the re-absorption loss aimed at the single-frequency laser emission. In fact, the experimental re-absorption loss and the threshold power may be between the two models' re-

sults. The reason is that there is spectral line width for both the pumping light and the coherent laser. Though the model two is more accurate than the model one owing to the energy degeneracy and Boltzmann constants, it is also based on the assumption that the pumping light and the coherent light are monochromatic. Therefore, both the two models offered the important data for laser design in different extent. According to the lab conditions, the spectrum line width of the 1152nm pumping light is less than 6nm, therefore, it is inferred that the model two is close to the experiment result. In addition, a problem worthy to be pointed out is that if the system parameters used are from the first model, they would also meet with the requirements of the model two.

### 3 Conclusions

In conclusion, two models were adopted for calculating the 1.2  $\mu\text{m}$  light's threshold power under the in-band pumped  $\text{Ho}^{3+}$ : LLF quasi-three-level system. Though many differences existed between the two models, it provided the experimental research with important data.

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